



No Calculator may be used on this section.

1. The scalar k is equal to 4. Vectors \mathbf{v}_1 and \mathbf{v}_2 are defined as $\mathbf{v}_1 = \langle -3, 5 \rangle$ and $\mathbf{v}_2 = \langle 2, -1 \rangle$.
Evaluate $k\mathbf{v}_1 + \mathbf{v}_2$. Then find the magnitude and direction of $k\mathbf{v}_1 + \mathbf{v}_2$.

$$4\langle -3, 5 \rangle + \langle 2, -1 \rangle$$

$$\langle -12, 20 \rangle + \langle 2, -1 \rangle = \langle -10, 19 \rangle$$

$$\text{Mag} = \sqrt{(-10)^2 + 19^2}$$

$$1. \sqrt{461}, \text{Central } 180^\circ - \tan^{-1}\left(\frac{19}{10}\right)$$

$$\begin{array}{r} 8 \\ 19 \\ \hline 177 \\ 19 \\ \hline 361 \end{array}$$

2. Find the unit vector in the direction of $(7, -24)$.

bearing
 $270 + \tan^{-1}\left(\frac{19}{10}\right)$

$$2. \left\langle \frac{7}{25}, -\frac{24}{25} \right\rangle$$

3. Let $\mathbf{u} = \langle -1, -1 \rangle$. Find the vector \mathbf{v} such that $\mathbf{u} \cdot \mathbf{v} = -6$ and $|\mathbf{v}| = \sqrt{18}$.

$$\mathbf{v} = \langle x, y \rangle \quad -x + -y = -6 \quad \sqrt{x^2 + y^2} = \sqrt{18}$$

$$\begin{aligned} x + y &= 6 \\ y &= 6 - x \end{aligned}$$

$$\begin{aligned} x^2 + (6-x)^2 &= 18 & 2x^2 - 12x + 18 &= 0 & \frac{3}{2} \\ x^2 + 36 - 12x + x^2 &= 18 & x^2 - 6x + 9 &= 0 & \frac{-18}{18} \\ 36 - 12x + 18 &= 18 & (x-3)^2 &= 0 & \\ -12x &= -18 & x &= 3 & \end{aligned}$$

$$\vec{v} = \left\langle \frac{3}{2}, \frac{9}{2} \right\rangle$$

$$\begin{aligned} y &= 6 - 3 \\ y &= 3 \\ y &= \frac{9}{2} \end{aligned}$$

$$x = \frac{18}{12} = \frac{3}{2} \quad \left\langle \frac{3}{2}, \frac{9}{2} \right\rangle$$

4. Which of the following vectors are orthogonal?

- A. $\langle 1, 2 \rangle$ and $\langle 2, 4 \rangle$
- B. $\langle 1, 2 \rangle$ and $\langle -1, -2 \rangle$
- C. $\langle -1, -2 \rangle$ and $\langle 1, -1 \rangle$
- D. $\langle -1, -2 \rangle$ and $\langle -2, 1 \rangle$ ✓

$$2 + -2 = 0$$

$$\langle 3, 3 \rangle$$

4. D